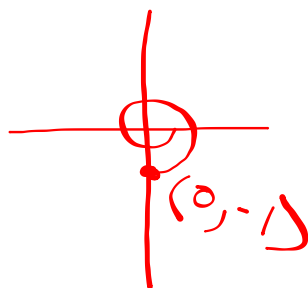


Warm-up 1/20/17

Find  $\sin \theta$ ,  $\cos \theta$ , and  $\tan \theta$ . $-450^\circ$  $-\frac{1}{0}$ 

$$\sin -450 = -1$$

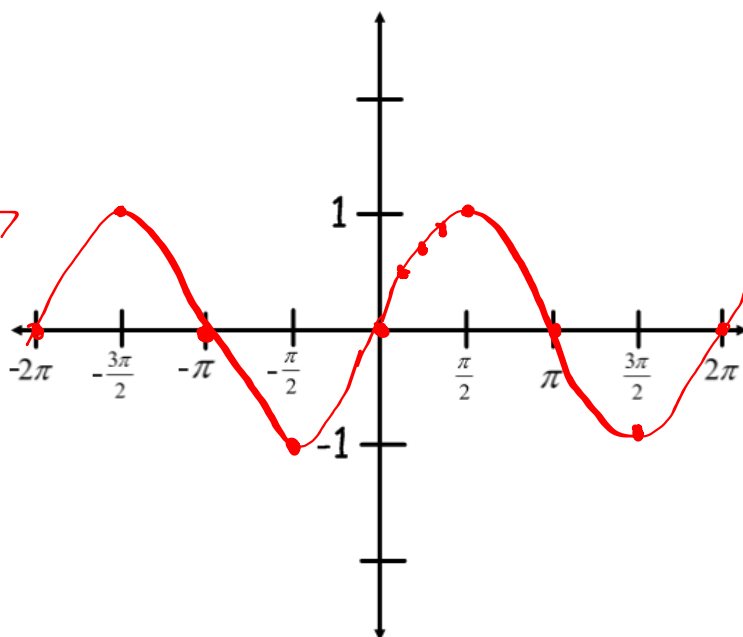
$$\cos -450 = 0$$

$$\tan -450 = \text{undefined}$$

#### 4.4: Graphs of Sine and Cosine: Sinusoids

Graph  $y = \sin x$ .

x	y
0	0
$\pi/6$	$1/2$
$\pi/4$	$\sqrt{2}/2 \approx .707$
$\pi/3$	$\sqrt{3}/2 \approx .866$
$\pi/2$	1
$\pi$	0
$3\pi/2$	-1
$2\pi$	0



DEFINITION: Sinusoid

A function is a **sinusoid** if it can be written in the form

$$f(x) = a \sin (bx + c) + d$$

where  $a$ ,  $b$ ,  $c$  and  $d$  are constants and neither  $a$  nor  $b$  is zero.

DEFINITION: Amplitude of a Sinusoid

The **amplitude** of the sinusoid  $f(x) = a \sin (bx + c) + d$  is  $|a|$ .

Similarly, the amplitude of  $f(x) = a \cos (bx + c) + d$  is  $|a|$ .

Graphically, the amplitude is half the height of the wave.

Find the amplitude of each function.

1)  $y = \sin x$

$$|1| = 1$$

2)  $y = \frac{1}{2} \sin x$

$$\left| \frac{1}{2} \right| = \frac{1}{2}$$

3)  $y = -3 \sin x$

$$|-3| = 3$$

Graphing Calculator



Period of a Sinusoid

The **period** of the sinusoid  $f(x) = a \sin (bx + c) + d$  is  $2\pi/|b|$ .

Similarly, the period of  $f(x) = a \cos (bx + c) + d$  is  $2\pi/|b|$ .

Graphically, the period is the length of one full cycle of the wave.

Find the period of each function.

$$1) y = \sin x \quad \frac{2\pi}{|1|} = 2\pi$$

$$2) y = -2\sin\left(\frac{x}{3}\right) \quad \frac{2\pi}{|1/3|} = 6\pi$$

$$3) y = 3\sin(-2x) \quad \frac{2\pi}{|-2|} = \pi$$

Frequency of a Sinusoid

The **frequency** of the sinusoid  $f(x) = a \sin (bx + c) + d$  is  $|b|/2\pi$ .

Similarly, the frequency of  $f(x) = a \cos (bx + c) + d$  is  $|b|/2\pi$ .

Graphically, the frequency is the number of complete cycles the wave completes in a unit interval.

Find the frequency of each function.

$$1) y = \sin x \quad \frac{|1|}{2\pi} = \frac{1}{2\pi}$$

$$2) y = -2\sin\left(\frac{x}{3}\right) \quad \frac{|1/3|}{2\pi} = \frac{1/3}{2\pi} = \frac{1}{6\pi}$$

$$3) y = 3\sin(-2x) \quad \frac{|-2|}{2\pi} = \frac{1}{\pi}$$

Assignment: pp. 357 - 359  
1 - 6, 15 - 18, 29